

# Planning for Steerable Bevel-tip Needle Insertion Through 2D Soft Tissue with Obstacles\*

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**Abstract**—We explore motion planning for a new class of highly flexible bevel-tip medical needles that can be steered to previously unreachable targets in soft tissue. Planning for these procedures is difficult because the needles bend during insertion and cause the surrounding soft tissues to displace and deform. In this paper, we develop a planning algorithm for insertion of highly flexible bevel-tip needles into soft tissues with obstacles in a 2D imaging plane. Given an initial needle insertion plan specifying location, orientation, bevel rotation, and insertion distance, the planner combines soft tissue modeling and numerical optimization to generate a needle insertion plan that compensates for simulated tissue deformations, locally avoids polygonal obstacles, and minimizes needle insertion distance. The simulator computes soft tissue deformations using a finite element model that incorporates the effects of needle tip and frictional forces using a 2D mesh. We formulate the planning problem as a constrained nonlinear optimization problem that is locally minimized using a penalty method that converts the formulation to a sequence of unconstrained optimization problems. We apply the planner to bevel-right and bevel-left needles and generate plans for targets that are unreachable by rigid needles.

**Index Terms**—steerable needle, medical robotics, motion planning, surgery simulation.

## I. INTRODUCTION

Needle insertion is a critical step in many diagnostic and therapeutic medical procedures, including biopsy to obtain a specific tissue sample for testing, drug injections for anesthesia, or radioactive seed implantation for brachytherapy cancer treatment. In this paper we consider highly flexible bevel-tip needles that can be steered around obstacles by taking advantage of needle bending and the asymmetric force applied by the needle tip to the tissue. These steerable needles are capable of reaching targets inaccessible by rigid needles.

The success of medical needle insertion procedures often depends on the accuracy with which the needle can be guided to a specific target in soft tissue. Unfortunately, inserting and retracting needles causes the surrounding soft tissues to displace and deform: ignoring these deformations can lead to significant errors. In brachytherapy, physicians use slightly flexible needles to permanently implant radioactive seeds inside the prostate that irradiate surrounding

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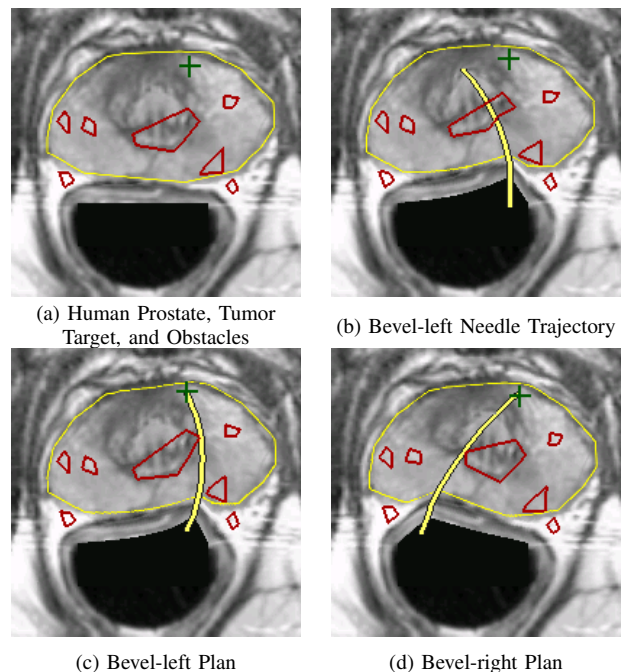


Fig. 1. In this example based on an MR image of the prostate [12], a biopsy needle attached to a rigid rectal probe (black half-circle) is inserted into the prostate (outlined in yellow) using simulation. Obstacles (red polygons) and the target (green cross) are overlaid on the image. The target is not accessible from the rigid probe by a straight line path without intersecting obstacles. However, bevel-tip needles bend as they are inserted into soft tissue (b). Our planner computes a locally optimal bevel-left needle insertion plan that reaches the target, avoids obstacles, and minimizes insertion distance (c). Using different initial conditions, our planner generates a plan for a bevel-right needle (d). Due to tissue deformation, the needle paths do not have constant curvature.

tissue over several months. Successful treatment depends on the accurate placement of radioactive seeds within the prostate gland [6], [15]. However, tissue deformations and needle bending lead to significant errors in seed implantation locations [15], [19], [1], [2].

Fast and accurate computer simulations of needle insertion procedures can facilitate physician training and assist in pre-operative planning and optimization. In this paper we develop a simulation and planner for steerable bevel-tip needle insertion in a 2D imaging plane. Many imaging methodologies, such as ultrasound, display a 2D planar cross-section of the human body. MR images, which may contain multiple planar slices composing a 3D volume, have an inter-slice distance significantly greater than the

diameter of a medical needle. Hence, in this paper we restrict needle motion to a 2D cross-section of the patient anatomy.

Our interactive simulation approximates soft tissues as linearly elastic materials and uses a 2D finite element model to compute tissue deformations due to tip and friction forces applied by the steerable needle. Polygonal obstacles represent tissues that cannot be cut by the needle, such as bone, or sensitive tissues that should not be damaged, such as nerves or arteries. The simulation enforces nonholonomic constraints on needle motion.

Our planner considers 4 degrees of freedom: initial location, initial orientation, binary bevel rotation, and insertion distance. The planner computes locally optimal values for these variables to compensate for tissue deformations and reach the target in simulation while avoiding polygonal obstacles and minimizing insertion distance so less tissue is damaged by the needle. Even in situations where real-time imaging such as ultrasound or interventional MRI is available, pre-planning is valuable to set the needle initial location and orientation and compute a desired trajectory that minimizes tissue damage.

## II. RELATED WORK

Needle insertion simulation requires estimating biomechanical deformations of soft tissue when forces are applied. Reviews of past work on finite element modeling for soft tissue simulation are included in [5] and [1].

Earlier work on interactive simulation of needle insertion assumed 2D planar deformations and a thin rigid needle with a symmetric tip [7], [3], [1]. Planning optimal insertion location and insertion distance to compensate for 2D tissue deformations has been addressed for rigid needles [2]. DiMaio and Salcudean modeled a flexible symmetric-tip needle with 2D triangular elements and used a nonlinear finite element method to compute the needle's deformation [8]. Key nodes from the needle mesh were embedded in a tissue mesh whose deformations were computed using a linear quasi-static finite element method.

Our interactive simulation relaxes both the needle rigidity and symmetric-tip assumptions by modeling steerable bevel-tip needles. Okamura et al. are studying paths of flexible bevel-tip needles during insertion [21]. O'Leary et al. showed that needles with bevel tips bend more than symmetric-tip needles [14]. Webster et al. developed thin highly flexible bevel-tip needles using Nitinol and experimentally tested them in very stiff tissue phantoms [21]. The needles followed constant-curvature paths in a plane when bevel rotation was fixed during needle insertion.

Webster et al. [21] developed a nonholonomic model for steering flexible bevel-tip needles in rigid tissues. The nonholonomic model, a generalization of a 3 degree-of-freedom bicycle model, was experimentally validated using a very stiff tissue phantom. Recent advances by Zhou and Chirikjian in nonholonomic path planning include stochastic model-based motion planning to compensate for noise bias [23] and probabilistic models of dead-reckoning error in nonholonomic robots [22].

Past work has addressed steering symmetric-tip needles in 2D deformable tissue that have 3 degrees of freedom: translating the needle base perpendicular to the insertion direction, rotating the the needle base along an axis perpendicular to the plane of the tissue, and translation along the needle insertion axis [8], [10]. DiMaio and Salcudean compute and invert a Jacobian matrix to translate and orient the base to avoid point obstacles with oval-shaped potential fields. Glozman and Shoham approximate the tissue using springs and also use an inverse kinematics approach to translate and orient the base every time step. In our work, we address bevel-tip steerable needles that have 2 degrees of freedom during insertion: rotation about the insertion axis and translation along the insertion axis. We are not aware of past work that has explicitly considered the effect of tissue deformations on this type of steerable needle.

Setting accurate parameters for tissue properties is important for realistic simulation. Krouskop et al. estimated the elastic modulus for prostate and breast tissue using ultrasonic elastography [13]. Past work has investigated friction models and parameters for needles in soft tissues [18], [11]. Physical measurements of forces exerted during needle insertion were measured by Kataoka et al., who separately measured tip and frictional forces during needle insertion into a canine prostate [11].

Medical needle insertion procedures may benefit from the more precise control of needle position and velocity made possible through robotic surgical assistants. A survey of recent advances in medical robotics was written by Taylor and Stoianovici [20]. Dedicated hardware for prostate biopsy needle insertion procedures that can be integrated with transrectal ultrasound imaging is being developed by Fichtinger et al. [9], [16].

## III. SIMULATION OF BEVEL-TIP NEEDLE INSERTION

A bevel-tip needle, unlike a symmetric-tip needle, will cut tissue at an angle, as shown in Fig. 2. Since the needle cuts at an angle away from the direction of insertion, the needle may bend in the direction of the bevel.

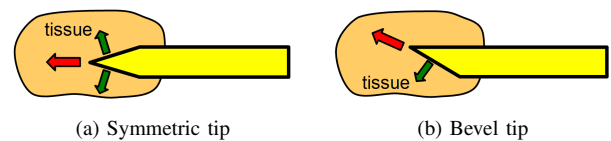


Fig. 2. A symmetric-tip needle exerts forces on the tissue equally in all directions, so it cuts tissue in the direction that the tip is moving. A bevel-tip needle exerts forces asymmetrically and cuts tissue at an angle.

In 2D, we only consider 2 bevel rotations: bevel-right ( $0^\circ$ ) and bevel-left ( $180^\circ$ ), as shown in Fig. 1. Rotating the bevel to different orientations will cause the needle tip to move out of the imaging plane. In future work, we plan to extend our 2D model to 3D and consider any bevel orientation in the range  $[0^\circ, 360^\circ)$ .

Our simulation models forces exerted by the needle on the soft tissue, including the cutting force at the needle tip and friction forces along the needle shaft. We assume

needle bending forces are negligible compared to the elastic forces applied by the soft tissue to the needle.

#### A. Soft Tissue Model

We specify the anatomy geometry (i.e. the prostate and surrounding tissues) using a finite element mesh. The geometric input is a 2D slice of tissue with tissue types segmented by polygons. We automatically generate a finite element mesh  $G$  composed of  $n$  nodes and  $m$  triangular elements in a regular right triangle mesh or using the constrained Delaunay triangulation software program Triangle [17], which generates meshes that conform to the segmented tissue type polygons.

The model must also include tissue material properties and boundary conditions for the finite element mesh. In our current implementation, we approximate soft tissues as linearly elastic, homogeneous, isotropic materials. For each segmented tissue type, the model requires tissue material properties (Young’s modulus, Poisson ratio, and density). We set values for these parameters as described in past work [2]. Mesh nodes inside bones are constrained to be fixed. A boundary condition of either free or fixed must be specified for each node on the mesh perimeter.

The complete tissue model  $M$  specifies the finite element mesh  $G$ , material properties, and boundary conditions. We assume the tissue in  $M$  is initially at equilibrium and ignore external forces not applied by the needle. We do not model physiological changes such as edema (tissue swelling), periodic tissue motion due to breathing or heart beat, or slip between tissue type boundaries.

#### B. Computing Soft Tissue Deformations

The *material mesh*  $G$  defines the geometry of the undeformed tissues, with each node  $i$  having coordinate  $\mathbf{x}_i$  in the material frame. Forces resulting from needle insertion cause the tissue to deform. The deformation is defined by a displacement  $\mathbf{u}_i$  for each node  $i$  in mesh  $G$ . The *deformed mesh*  $G'$  is constructed in the world frame using the displaced node coordinate  $\mathbf{x}_i + \mathbf{u}_i$  for each node  $i$ . A point  $\mathbf{y}$  in the material frame can be transformed to the world frame coordinate  $\mathbf{y}'$  and vice versa using linear interpolation between the nodes of the enclosing finite element [1].

At each time step of the simulation we compute the acceleration of each node  $i$ , which includes acceleration due to elastic forces computed using a linear finite element method and the external force  $\mathbf{f}_i$  exerted by the needle. We use explicit Euler time integration to integrate velocity and displacement for each free node for each time step. Time steps have duration  $h = 0.01$  seconds.

#### C. Needle Insertion Model

Without loss of generality, we set the coordinate axes of the world frame so that the default needle insertion axis is along the positive  $z$ -axis. The  $y$ -axis corresponds to the initial location degree of freedom. The needle tip is initially located at a base coordinate  $\mathbf{p}_0 = (y_0, z_0)$ . The initial orientation of the needle is specified using  $\theta$ , as shown

in Fig. 3. For simulation stability, we constrain  $\theta$  between  $-45^\circ$  and  $45^\circ$ . The needle tip rotation is either bevel-right ( $0^\circ$ ) or bevel-left ( $180^\circ$ ). We assume the needle tip rotation is held constant during insertion due to planner efficiency and lack of experimental data for simulation, although we hope to relax this assumption in future work.

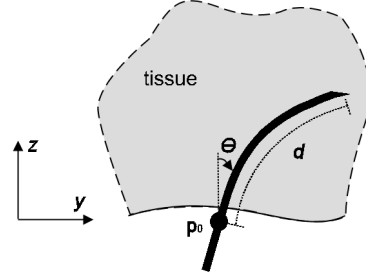


Fig. 3. Slice of soft tissue in the  $yz$  plane. The bevel-tip needle is initially at the base coordinate  $\mathbf{p}_0$  with orientation  $\theta$ . It is inserted a distance  $d$ , causing the surrounding soft tissue to deform.

We assume the flexible needle is supported so that it does not bend outside the tissue. Once the needle has entered the tissue, it will bend in the direction of the bevel-tip. The distance the needle has been inserted from the base coordinate is  $d$ . We parameterize the needle by  $s$  where  $s = 0$  corresponds the needle base and  $s = d$  corresponds to the needle tip. Let  $\mathbf{p}_s$  denote the material frame coordinate of the point along the needle a distance  $s$  from the base.

Simulation of needle insertion requires a needle model  $N$  that specifies needle properties, including insertion velocity  $v$ , the cutting force required at the needle tip to cut tissue, and the static and dynamic coefficients of friction between the tissue and needle.

We model the needle by line segment elements that correspond to edges of triangle elements in the deformed tissue mesh. Since the needle path is not known a priori, the material mesh must be modified in real-time. The simulation maintains a node at the needle tip location and a list of nodes along the needle shaft. At each simulation time step, the needle exerts force on the tissue at the needle tip, where the needle is displacing and cutting the tissue, and along the needle shaft due to friction.

Highly flexible bevel-tip needles tested in tissue phantoms by Webster et al. [21] were experimentally shown to follow a constant-curvature path when the bevel rotation was fixed during needle insertion. Setting simulation parameters to the limiting case of highly stiff tissue, zero tissue cutting force, and zero friction allows us to replicate this constant curvature path. In other cases, the needle path through deformed tissue may not be of constant curvature.

#### D. Simulating Cutting at the Needle Tip

During each simulation time step, the needle tip moves a distance  $vh$  in the world frame, where  $v$  is the needle insertion velocity and  $h$  is the time step duration. The simulation must maintain element edges along the needle path, which requires mesh modification as the needle cuts through the tissue.

The simulation constrains a node to be located at the needle tip. The current needle tip node is labeled  $n_{tip}$  and the needle is pointed in direction  $\mathbf{q}$ . The needle will cut tissue a small distance  $d_{cut}$  along the vector  $\mathbf{r}$  in the world frame, where  $\mathbf{r}$  is deflected from  $\mathbf{q}$  by an angle  $\theta_d$ , as shown in Fig. 4. If the force at the needle tip along  $\mathbf{r}$  is greater than a threshold  $f_{cut}$  based on needle and tissue properties, then the needle will cut through the tissue. Cutting is represented in the material mesh by moving the needle tip node  $n_{tip}$  by the distance  $d_{cut}$  transformed to the material frame. If no tissue deformation occurs, this method guarantees the needle will cut a path of constant curvature whose radius of curvature is a function of the deflection angle  $\theta_d$ . When tissue deformation does occur at the needle tip, the path will be of constant curvature locally but will deviate from constant curvature globally depending on the magnitude of the deformations.

As the needle tip cuts through the mesh, it will be necessary to change the needle tip node. If the needle tip node is too close to the opposite triangle edge  $e$ , the tip node is moved back along the shaft and a new tip node, the closest node along edge  $e$ , is selected as the new tip node and moved to the new tip location in the material frame.

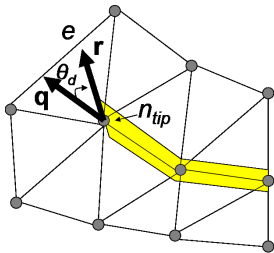


Fig. 4. The tissue mesh is modified so edge boundaries are formed along the path of needle insertion. A subset of the tissue mesh, centered at needle tip node  $n_{tip}$ , is shown. The straight line path of the needle is shown by vector  $\mathbf{q}$ . Because of the bevel-tip, the needle cuts tissue in direction  $\mathbf{r}$ , which is deflected from  $\mathbf{q}$  by  $\theta_d$  degrees.

### E. Simulating Friction Along the Needle Shaft

We implemented a stick-slip friction model between the needle and the soft tissue. Nodes along the needle shaft carry friction state information; they are either attached to the needle (in the static friction state) or allowed to slide along the needle shaft (in the dynamic friction state).

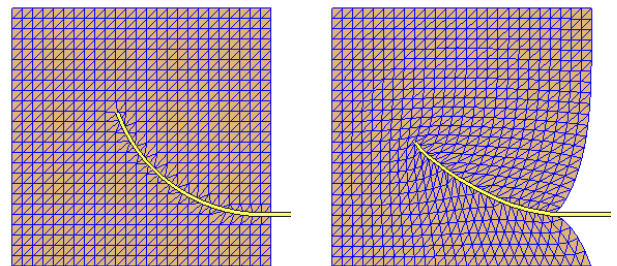
When a node enters the static friction state, its distance from the needle tip along the shaft is computed. For each time step where the node remains in the static friction state, its position is modified by moving it tangent to the needle so that its distance from the tip along the needle shaft is held constant. A node moves from the static to the dynamic friction state when the force required to displace the node along the needle shaft exceeds a slip force parameter  $f_{s,max}$ .

When a node is in the dynamic friction state, a dissipative force is applied along the needle tangent. A node moves from the dynamic to the static friction state when the relative velocity of the needle to the tissue at the node is close to zero.

### F. Simulation Results

Our simulator was implemented in C++ using OpenGL for visualization. It achieved an average of approximately 100 frames per second on a 1.6GHz Pentium M computer for a mesh composed of 1250 triangular elements. Computation time per frame increases linearly with the number of nodes along the needle shaft.

We demonstrate our simulation results in 2 cases: rigid tissue and deformable tissue. In both cases we simulate the insertion of a bevel-tip needle into a square of tissue fixed on 3 sides. In the first case, we consider tissue that is stiff relative to the needle and a sharp frictionless bevel-tip needle that cuts the tissue with zero cutting force. As shown in Fig 5(a), the simulated needle follows a path of constant curvature, which is the behavior experimentally verified by Webster et al. [21]. In the second case shown in Fig. 5(b), we insert the needle into a deformable soft tissue mesh with positive cutting force and friction coefficients. Although the tip locally follows a path of constant curvature as explained in Section III-D, the global path is not of constant curvature. Past experiments have demonstrated the effect of tissue deformations due to rigid needle insertion [7], [1]. We plan to develop experiments to test the bending behavior of flexible bevel-tip needles in deformable tissues to more accurately set parameters for our model in future work.



(a) Rigid Tissue

(b) Deformable Tissue

Fig. 5. We simulate insertion of a bevel-tip needle into a square tissue fixed on 3 sides. When the tissue is stiff relative to the needle, a sharp frictionless needle cuts a path of constant curvature (a). A needle with positive cutting and friction forces will bend in deformable tissue (b).

## IV. PLANNING

A needle insertion plan is defined by  $X = (y_0, \theta, b, d)$  where  $y_0 \in \mathbb{R}$  is the insertion location,  $\theta \in [-90^\circ, 90^\circ]$  is the insertion angle,  $b \in \{0^\circ, 180^\circ\}$  is the bevel rotation, and  $d \in \mathbb{R}^+$  is the distance the needle will be inserted. Obstacles are defined as nonoverlapping polygons in a set  $O$ . The target is defined as a point  $t$  in the material frame of the soft tissue mesh. A plan  $X$  is feasible if the needle tip is within  $\epsilon_t > 0$  of the target and the needle path in deformable tissue does not intersect any obstacle. The goal of needle insertion planning is to generate a feasible plan  $X$  that minimizes  $d$ .

### A. Problem Formulation

The simulation of needle insertion described in Section III takes parameters  $X$  for the initial conditions and needle

insertion distance,  $M$  for the soft tissue model, and  $N$  for the needle model and outputs the coordinates  $\mathbf{p}_s$  for  $s \in [0, d]$  that the needle will follow in the material frame.

$$\mathbf{p}_s = \text{NeedleSim}(X, M, N), s \in [0, d]$$

The variables of plan  $X$  are constrained by application specific limits  $y_{min}$ ,  $y_{max}$ ,  $\theta_{min}$ ,  $\theta_{max}$ , and  $d_{max}$ .

$$\begin{aligned} y_{min} &\leq y_0 \leq y_{max} \\ \theta_{min} &\leq \theta \leq \theta_{max} \\ 0 &\leq d \leq d_{max} \end{aligned}$$

These constraints enforce the limits of the simulation, such as the angle requirements in Section III-C. In the biopsy example in Fig. 1,  $d_{max}$  is the maximum length of the needle and  $y_{max} - y_{min}$  defines the width of the rectal probe.

The needle tip coordinate  $\mathbf{p}_d$  in a feasible solution must be within Euclidean distance  $\epsilon_t$  of the target  $\mathbf{t}$ .

$$\|\mathbf{p}_d - \mathbf{t}\| \leq \epsilon_t$$

In the presence of a nonempty set of polygonal obstacles  $O$ , we require that the needle path in a feasible solution does not intersect an obstacle. Let  $c_s$  be the distance from  $\mathbf{p}_s$  to the closest point on the closest obstacle  $o \in O$  and let the sign of  $c_s$  be negative if  $\mathbf{p}_s$  is inside obstacle  $o$  and positive otherwise. We require  $c_s \geq \epsilon_o$  for some given tolerance  $\epsilon_o \geq 0$  for all points  $s$  along the needle shaft. We formulate this constraint as

$$\int_0^d \max\{-c_s + \epsilon_o, 0\} ds \leq 0.$$

We can quickly compute this integral numerically using points sampled along the needle path.

We summarize the problem formulation for variable  $X = (y_0, \theta, b, d)$  given target coordinate  $\mathbf{t}$ , polygonal obstacles  $O$ , tolerances  $\epsilon_t$  and  $\epsilon_o$ , tissue model parameters  $M$ , needle model parameters  $N$ , and variable limits  $y_{min}$ ,  $y_{max}$ ,  $\theta_{min}$ ,  $\theta_{max}$ , and  $d_{max}$ .

$$\begin{aligned} \min f(X) &= d \\ \text{Subject to:} \\ \|\mathbf{p}_d - \mathbf{t}\| &\leq \epsilon_t \\ \int_0^d \max\{-c_s + \epsilon_o, 0\} ds &\leq 0 \\ y_{min} &\leq y_0 \leq y_{max} \\ \theta_{min} &\leq \theta \leq \theta_{max} \\ 0 &\leq d \leq d_{max} \end{aligned}$$

The values of  $\mathbf{p}_s$  for  $s \in [0, d]$  are computed by executing the simulator  $\text{NeedleSim}(X, M, N)$ . The obstacle distances  $c_s$  for  $s \in [0, d]$  are computed using  $\mathbf{p}_s$  and the set of obstacles  $O$ .

### B. Optimization Method

To reduce the complexity of the optimization, we reduce the number of variables in  $X$  from 4 to 2. Given a plan  $X$ , we can find the optimal insertion distance  $d$  by executing the simulation to insertion distance  $d_{max}$  and identifying the point  $\mathbf{p}_s$  along the needle path that minimizes the

distance to the target  $\mathbf{t}$ . Hence,  $d$  does not need to be explicitly treated as a variable since its value is implied by the other variables in  $X$ . Furthermore, variable  $b$  in  $X$  is binary since it represents the bevel-right or bevel-left needle rotation state. We optimize  $X$  separately for the bevel-right and bevel-left states.

We solve for a locally optimal solution  $X^*$  using a penalty method. Penalty methods, originally developed in the 1950's and 1960's, solve a constrained nonlinear optimization problem by converting it to a series of unconstrained nonlinear optimization problems [4]. Given the constrained optimization problem  $\min f(\mathbf{x})$  subject to  $g(\mathbf{x}) \leq 0$ , we can write the unconstrained problem  $\min(f(\mathbf{x}) + \mu \max\{0, g(\mathbf{x})\}^2)$  for some large  $\mu > 0$ . Penalty methods generate a series of unconstrained optimization problems as  $\mu \rightarrow \infty$ . Each unconstrained optimization problem can be solved using Gradient Descent or variants of Newton's Method. For convex nonlinear problems, the method will generate points that converge arbitrarily close to the global optimal solution [4]. For nonconvex problems, the method can only converge to a local optimal solution.

For steerable needle insertion planning, we convert the target and obstacle constraints to penalty functions to define a new nonlinear nonconvex optimization problem.

$$\begin{aligned} \min \hat{f}(X) &= d + \mu (\max\{\|\mathbf{p}_d - \mathbf{t}\| - \epsilon_t, 0\})^2 + \\ &\quad \mu \left( \int_0^d \max\{-c_s + \epsilon_o, 0\} ds \right)^2 \end{aligned}$$

Subject to:

$$\begin{aligned} y_{min} &\leq y_0 \leq y_{max} \\ \theta_{min} &\leq \theta \leq \theta_{max} \\ 0 &\leq d \leq d_{max} \end{aligned}$$

Evaluating the objective function  $\hat{f}(X)$  requires executing the simulator  $\text{NeedleSim}(X, M, N)$  to compute the needle path  $\mathbf{p}_s$  for  $s \in [0, d]$  and the obstacles distances  $c_s$ . The remaining constraints are the limit constraints that are required for simulation stability and can never be violated.

We use Gradient Descent to find a local optimal solution to the unconstrained minimization problem  $\min \hat{f}(X)$ . The limit constraints are easily enforced at each iteration. We solve a sequence of 4 unconstrained problems, each with 10 Gradient Descent iterations. After each unconstrained problem has been solved, we multiply the penalty factor  $\mu$  by 10. In future work, we plan to determine problem-specific termination criteria for the unconstrained optimization problems and for the penalty method.

The objective function  $\hat{f}(X)$  cannot be directly differentiated since the simulator cannot be written as a closed form equation. For the Gradient Descent method, we numerically approximate the derivatives of the objective function with respect to the insertion location  $y_0$  and orientation  $\theta$ . We compute  $d\hat{f}/dy_0$  by translating the needle path by  $\Delta y_0$  and recomputing  $\hat{f}$ . Similarly, we compute  $d\hat{f}/d\theta$  by rotating the needle path by  $\Delta\theta$  about the insertion base coordinate  $\mathbf{p}_0$  and recomputing  $\hat{f}$ . These approximations do not explicitly account for the different deformations that occur when  $y_0$  or  $\theta$  are modified but were sufficiently

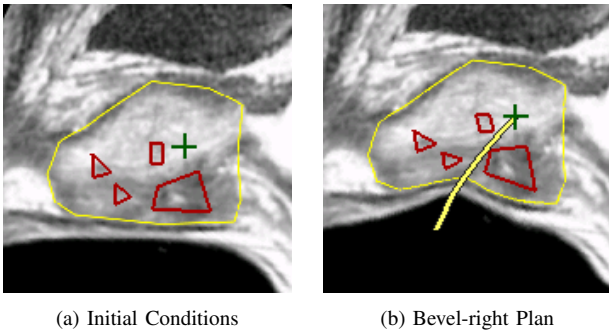


Fig. 6. In this example based on an MR image of the sagittal plane of the prostate [12], a biopsy needle is inserted into the prostate (outlined in yellow) (a). The planner computes an initial position, orientation, and insertion distance so the needle reaches the target (green cross) while avoiding obstacles (red polygons) and compensating for tissue deformations in simulation (b).

accurate for small  $\Delta y_0$  and  $\Delta\theta$  in our results described below.

### C. Planner Results

We implemented the planner in C++ and used the simulation described in Section III. Results for medical biopsy examples are shown in Fig. 1(c), Fig. 1(d), and Fig. 6(b). For each example, the tissue model mesh was composed of 1196 triangular elements and the planner required approximately 5 minutes of computation time on a Pentium M 1.6GHz computer. We set  $\epsilon_t = \epsilon_o = 0.1\text{cm}$  and the penalty method solution satisfied the constraints within a tolerance of 0.02.

## V. CONCLUSION

We described a needle insertion planning algorithm for steerable bevel-tip needles that combines numerical optimization with soft tissue simulation. The simulation, based on a linear finite element method, models the effects of needle tip and frictional forces on soft tissues defined by a 2D mesh. Our planning algorithm computes a locally optimal initial location, orientation, and insertion distance for the needle to compensate for predicted tissue deformations and reach a target while avoiding polygonal obstacles.

The effectiveness of the planner is dependent on the accuracy of the simulation of steerable needle insertion and soft tissue deformations. In future work, we will compare the output of our simulation to new physical experiments, determine the sensitivity of results to model parameters, consider a finite set of different bevel types, allow bevel rotation during insertion, improve the efficiency of our optimization method, and extend our simulation and planner to 3D.

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